

Measuring Cost and Risk of Public Debt: Use of an ALM Framework

Based on Client Presentation

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*Drawing substantially on a presentation
prepared by the World Bank*

Debt Profile: Summary of the portfolio's current risk position using a set of indicators

- Market Risk
 - external debt/total debt
 - currency structure
 - floating interest rate debt/total debt
 - duration
 - average life
 - amortization schedule
 - amount or percentage of principal payments due each period
- Fiscal sustainability
 - Total debt/GDP
 - Total debt/tax revenues
 - Debt service/total revenues
 - New borrowings/debt
- BoP sustainability
 - External debt/Exports
 - External debt service/exports

Debt Profile is a Summary - not a Risk Measure

- A debt profile is a set of indicators that imply potential volatility of debt servicing
- Most government debt offices use cash flow simulations to measure cost and risk of debt
 - Cost is measured as the future debt servicing costs
 - Risk is measured as the potential increase in costs
 - But risk is a relative concept and it is useful to have a framework for modeling it

Government ALM Framework

- An ALM framework examines the nature of the government's assets and liabilities, with the objective of reducing overall risk for the government
- Risk of the government's liabilities is measured relative to the government's assets, and its objectives for managing those assets
- This approach facilitates risk management by matching assets and liabilities (natural hedging), and providing a framework for measuring costs and risks

Simplified sovereign balance sheet

Assets	Liabilities
PV of future taxes	Debt
	PV of future expenditures (excluding debt service)

$PV \text{ of future taxes} - PV \text{ of future expenditures} = PV \text{ of debt}$

In this framework, debt is the equivalent of deferred taxes

Risk Implications of the Simplified Balance Sheet

- Balance sheet risk is minimised when risk characteristics of debt matches that of future taxes minus future government expenditures ($T - G =$ the primary surplus)

If T and G are largely in domestic currency, risk is minimised when debt is in domestic currency

As $(T - G)$ is relatively insensitive to real interest rates, risk is minimised by issuing long-term, fixed rate debt (long duration)

If domestic debt market is relatively undeveloped \Rightarrow trade-off between long-duration FX debt vs. short-duration domestic debt

Best debt strategy requires measuring cost and risk of trade-offs

Managing risk on a sub-portfolio basis

Assets		Liabilities
Foreign exchange reserves	←→	Foreign exchange debt
PV of tax revenues	←→	Long-term, fixed rate, domestic currency debt

- balance sheet risk is minimised by: matching the FX composition and interest rate characteristics of FX debt with FX reserves
- issuing the rest in long maturity, fixed rate domestic currency debt

Methodology for Measuring Cost & Risk

Pure ALM methodology: for each debt strategy, simulate a range of paths of possible future debt servicing costs & future government revenues or primary surplus

- If the two flows move together when market prices change (i.e. sensitivity of A&L to market variables is the same), the liability portfolio is immunized
- Otherwise, debt servicing costs will be volatile relative to revenues. Risk is measured as the volatility.

Methodology for Measuring Cost & Risk

- BUT: the joint modeling of debt servicing costs and revenues is highly complex
 - Requires jointly modeling interest and exchange rates, macro variables and the government's assets and liabilities
 - A few debt offices (Sweden, Brazil, UK) have begun experimenting with this approach
- Most debt offices simplify the process by comparing the range of future debt servicing costs against a notional reference representing the government's main assets
 - Assume assets denominated in local currency and of long duration.
 - Implies risk should be measured in terms of volatility of debt service in local currency over the medium- to long-term

Step 1: Determine the cost

Step 1

- Debt service cost flows are projected forward for a medium- to long-term horizon under base case assumptions of the funding strategy and future market rates
- The base case assumptions of future market rates should be “market-neutral”; e.g.:
 - Based on survey of market participants
 - Derived from implied currency and interest rate forwards
 - Simple assumptions that rates remain constant
- The cost is measured as annual debt servicing costs under base case assumptions
 - Total debt service; or as a proportion GDP (proxy for power to tax)

Step 2: Design risk scenario

Step 2

- New projections are made under alternative market rate assumptions
- These alternative cases can be generated using
 - statistical techniques
 - historical analysis
 - “worst case” scenarios, etc.

Step 3: Measure risk

Step 3

- Risk is measured as the volatility or potential increase of debt servicing costs relative to the base case
- Risk can be modeled using deterministic scenarios or stochastic simulations
- Best to start with simple scenario models and move to stochastic simulation later
 - Scenario models handle economic shocks more easily (stochastic models tend to assume normally distributed variables; real world variables have “fat-tails”)
 - Try to consider impact of shocks on GDP and primary surplus as well as interest and exchange rates – step towards integrated macro model

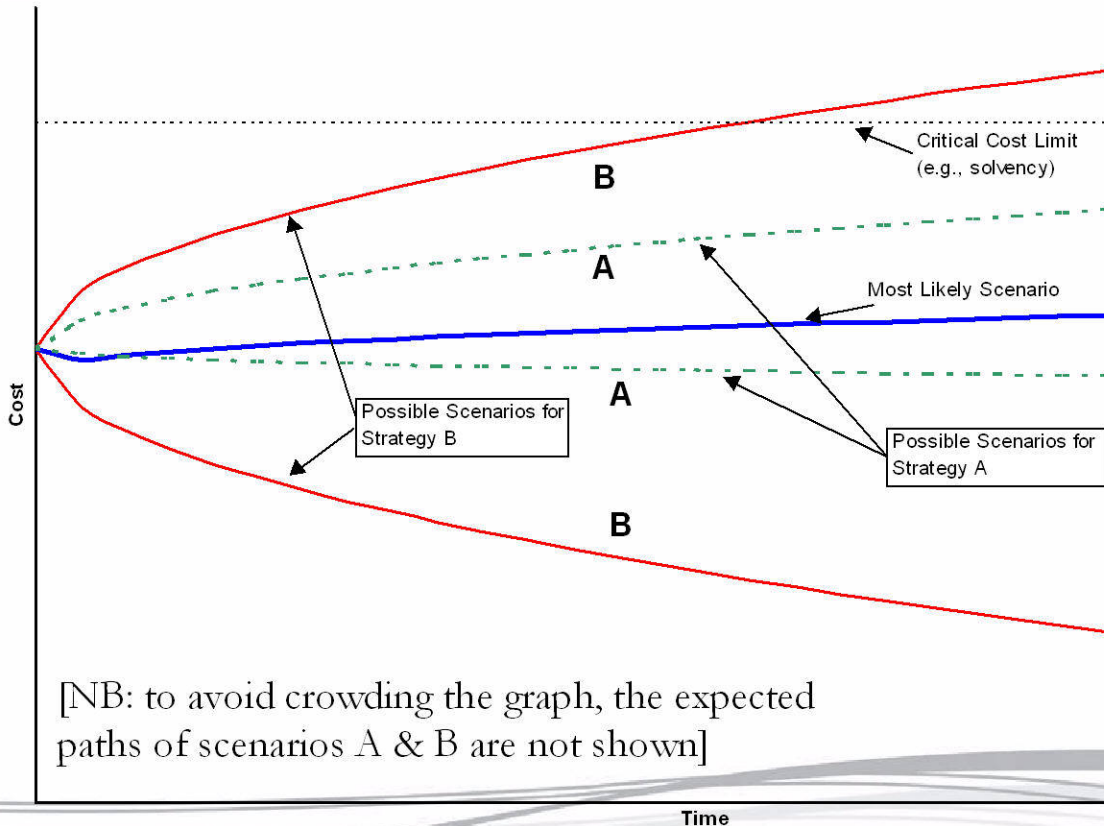
Step 4: Repeat process for other strategies

Step 4

- Steps 1 - 3 are repeated for alternative funding strategies, and costs and risks of strategies are compared
- e.g., strategy A: 75% fixed, 25% floating; strategy B: 25% fixed, 75% floating
- [if available] explore impact of index-linked bonds – more resilient in event of demand shocks

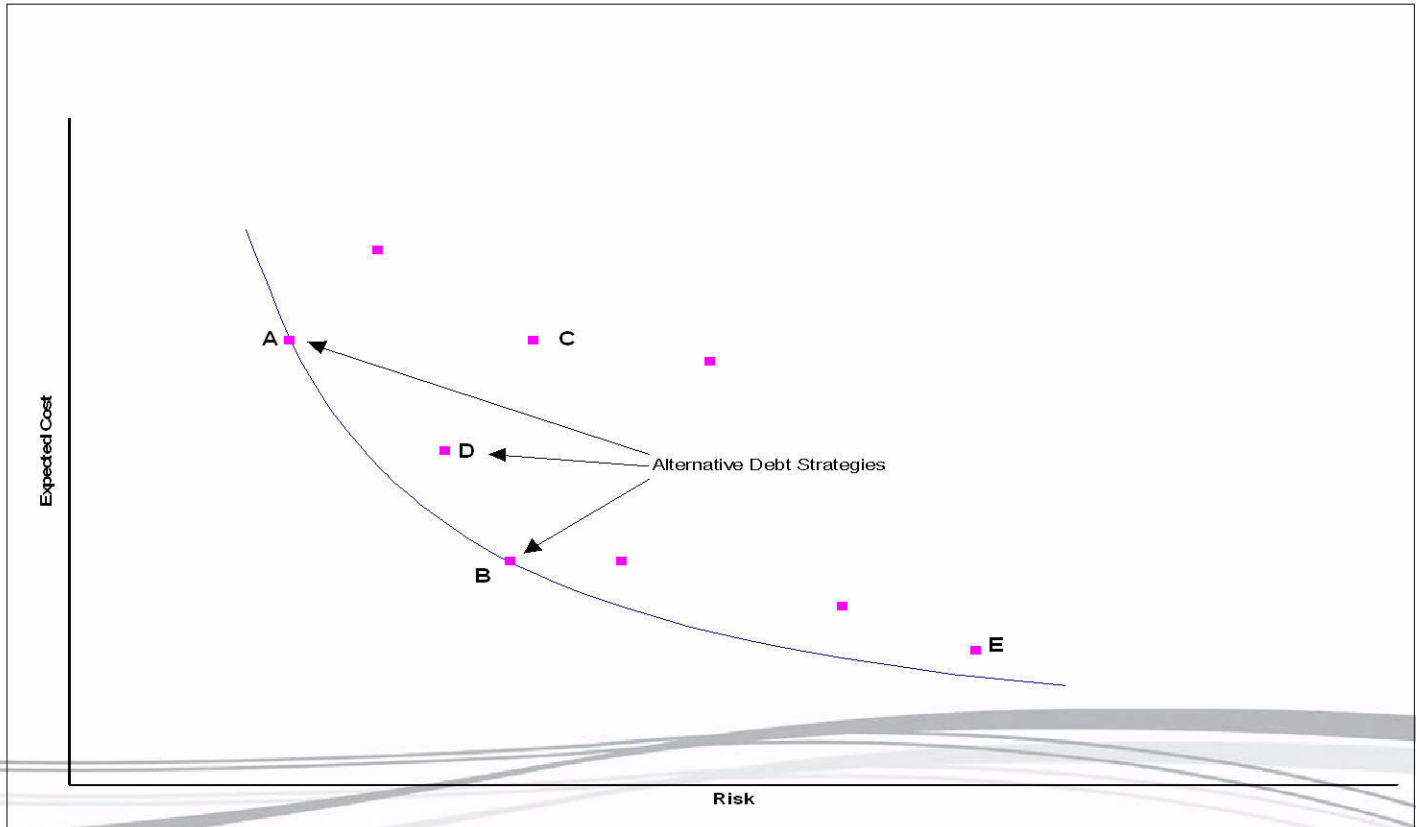
Expected Cost and Risk

Cost Consideration for Alternate Strategies



[NB: to avoid crowding the graph, the expected paths of scenarios A & B are not shown]

The Costs and Risks of Alternative Strategies are Compared



Step 5: Select the Strategy

Step 5

- These models are not “optimisation” models, but merely present information on the costs and risks of the alternative strategies to the decision makers
- The strategy is selected on the basis of the risk tolerance of the government

Note on Tax Smoothing

- Hedging against exogenous shocks to the government's finances, to avoid unexpected changes in taxes.
- Supply shocks
 - negative correlation prices and real output
 - positive correlation return on nominal debt and tax revenues
- Demand shocks
 - positive correlation prices and output.
 - nominal debt adds to variation – cost of nominal debt rises when output and tax revenue fall
- Effects increase as maturity of debt lengthens - persistent changes in price level have greater effect on LT than ST debt
- Advantage of index-linked debt for economy subject to demand shocks (e.g. UK in past)